

# PURCHASE SIGNATURES OF RETAIL CUSTOMERS

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# Motivations

- Retailers have a lot of data on customers purchases
- Detecting **individual customer habits** is crucial
  - Personalized marketing
  - Attrition detection/characterization
- Challenges
  - Customers are not perfectly regular
  - Dataset size (~300 GB)

# Motivations

- How often does a customer replenish his/her products?
  - Give coupon on the **right product** at the **right time**
  - Strong **attrition signal** on favourite products
- Find the favourite products of a customer
- Find the replenishment period

# Existing methods

- Pattern mining methods
  - Top-k [6]
  - Periodic pattern [5]
  - Frequent itemsets [1]
  - Episode mining [9]
- Item recommendation methods
- Drawbacks
  - Many results
  - Regularity definition too strict or too loose
  - Products have to be bought in the same transaction
  - Non interpretable models

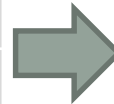
# Proposed model: signatures

- Find favourite products of a customer
  - Bought several times
  - **Not** necessarily in the **same transaction**
- Find **recurrent symbols** and their **occurrences** in a symbolic sequence, with no predefined period
  - **A set** of product and its **occurrences** as results
  - Period adapts to the sequence rhythm

# Signature model – Sequence segmentation

- k-segmentation [8]: split a sequence of n transactions into k segments

Timestamp	Receipts
1	Bread, Milk, Orange Juice, Soup
2	Butter, Apple, Soup, Orange Juice
3	Bread, Sponge
4	Bread, Butter, Soup
5	Orange Juice, Eggs
6	Bread, Milk, Eggs



Timestamp	Receipts
1	Bread, Milk, Orange Juice, Soup
2	Butter, Apple, Soup, Orange Juice
3	Bread, Sponge
4	Bread, Butter, Soup
5	Orange Juice, Eggs
6	Bread, Milk, Eggs

A 3-segmentation of a customer purchase sequence

# Signature model – Sequence segmentation

- Segment representative:  $\mu(S_i) = \bigvee_{t \in S_i} t$

	Timestamp	Receipts
S1	1	Bread, Milk, Orange Juice, Soup
	2	Butter, Apple, Soup, Orange Juice
S2	3	Bread, Sponge
	4	Bread, Butter, Soup
S3	5	Orange Juice, Eggs
	6	Bread, Milk, Eggs



Segment index	Segment representatives $\mu(S_i)$
1	Bread, Milk, Orange Juice, Soup, Butter, Apple
2	Bread, Butter, Soup, Sponge
3	Bread, Orange Juice, Eggs, Milk

# Signature model – Sequence segmentation

- Adequation:  $A(\alpha, S) = |\bigwedge_{S_i \in S} \mu(S_i)|$

Segment index	Segment representatives $\mu(S_i)$
1	Bread, Milk, Orange Juice, Soup, Butter, Apple
2	Bread, Butter, Soup, Sponge
3	Bread, Orange Juice, Eggs, Milk

- $A(\alpha, S) = |\bigwedge_{S_i \in S} \mu(S_i)| =$   
 $|\{Bread, Milk, Orange Juice, Soup, Butter, Apple\} \cap$   
 $\{Bread, Butter, Soup, Sponge\} \cap$   
 $\{Bread, Orange Juice, Eggs, Milk\} = |\{Bread\}| = 1$

Segment index	Segment representatives $\mu(S_i)$
1	<b>Bread</b> , Milk, Orange Juice, Soup, Butter, Apple
2	<b>Bread</b> , Butter, Soup, Sponge
3	<b>Bread</b> , Orange Juice, Eggs, Milk



# Signature model – Sequence segmentation

- $S_{opt}(\alpha, k) = \arg \max_{S \in \mathcal{S}_{n,k}} A(\alpha, S)$

Timestamp	Receipts
1	Bread, Milk, Orange Juice, Soup
2	Butter, Apple, Soup, Orange Juice
3	Bread, Sponge
4	Bread, Butter, Soup
5	Orange Juice, Eggs
6	Bread, Milk, Eggs

+  $k = 3$

- Solve  $S_{opt}(\alpha, k)$

# Signature model – Sequence segmentation

	Timestamp	Receipts
S1	1	Bread, Milk, Orange Juice, Soup
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S2	3	Bread, Sponge
	4	Bread, Butter, Soup
S3	5	Orange Juice, Eggs
	6	Bread, Milk, Eggs



Segment index	Segment representatives $\mu(S_i)$
1	<b>Bread</b> , Milk, Orange Juice, Soup, Butter, Apple
2	<b>Bread</b> , Butter, Soup, Sponge
3	<b>Bread</b> , Orange Juice, Eggs, Milk

$$A(\alpha, S) = |\{Bread\}| = 1$$

# Signature model – Sequence segmentation

	Timestamp	Receipts
S1	1	Bread, Milk, Orange Juice, Soup
	2	Butter, Apple, Soup, Orange Juice
S2	3	Bread, Sponge
	4	Bread, Butter, Soup
S3	5	Orange Juice, Eggs
	6	Bread, Milk, Eggs



Segment index	Segment representatives $\mu(S_i)$
1	<b>Bread, Milk, Orange Juice, Soup</b>
2	<b>Bread, Apple, Sponge, Orange Juice, Butter, Soup</b>
3	<b>Bread, Orange Juice, Eggs, Milk</b>

$$A(\alpha, S) = |\{Bread, Orange Juice\}| = 2$$

# Signature model – Sequence segmentation

	Timestamp	Receipts
S1	1	Bread, Milk, Orange Juice, Soup
S2	2	Butter, Apple, Soup, Orange Juice
	3	Bread, Sponge
S3	4	Bread, Butter, Soup
	5	Orange Juice, Eggs
	6	Bread, Milk, Eggs



Segment index	Segment representatives $\mu(S_i)$
1	<b>Bread, Milk, Orange Juice, Soup</b>
2	<b>Bread, Apple, Sponge, Orange Juice, Butter, Soup</b>
3	<b>Bread, Orange Juice, Eggs, Milk, Soup</b>

$$A(\alpha, S) = |\{Bread, Orange Juice, Soup\}| = 3 = \arg \max_{S \in \mathcal{S}_{6,3}} A(\alpha, S)$$

# Signature model – Sequence segmentation

- Mining algorithms: exact approaches
  - Dynamic programming  $O(n^2k)$
  - Pattern growth  $O(2^{|I|})$
- Mining algorithms: other approaches
  - Greedy algorithms  $O(n * \log(n))$
  - Non exact algorithms with bounded error  $O(n^{\frac{4}{3}}k^{\frac{5}{3}})$

# Signature model – Sequence segmentation

- $T_i$  is a boolean vector
  - $(p_1, p_2) = (1, 1, 0, 0)$  with 4 products
- $\mu(S_i) = \bigvee_{t \in S_i} t$
- $A(\alpha, S) = \left| \bigwedge_{S_i \in S} \mu(S_i) \right|$
- $S_{opt}(\alpha, k) = \arg \max_{S \in \mathcal{S}_{n,k}} A(\alpha, S) \rightarrow$  optimized with **dynamic programming** [8]

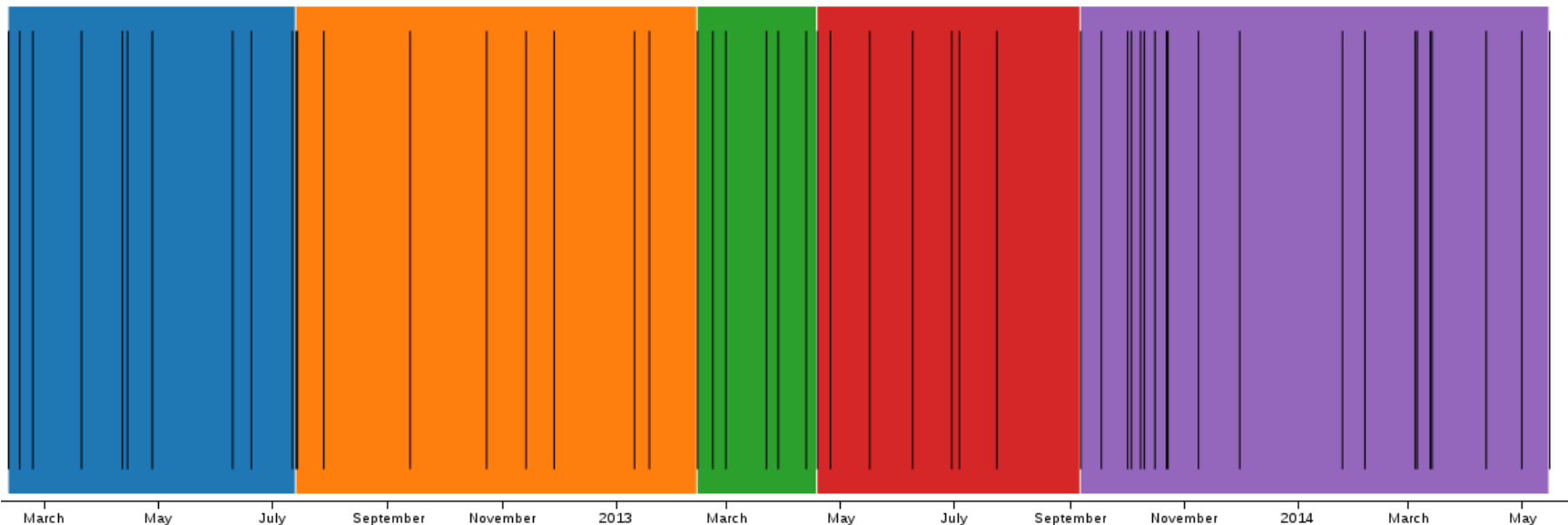
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2	Butter, Apple, Soup, Orange Juice
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4	Bread, Butter, Soup
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6	Bread, Milk, Eggs

+ {*Bread, Orange Juice, Soup*}

# Signature - example

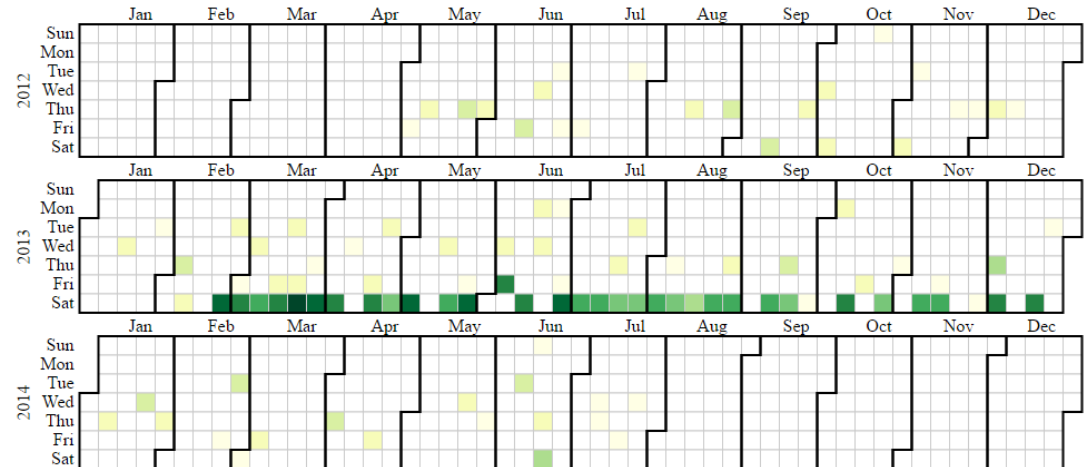
- JOKER MULTIFRUIT BRK OVALINE1L
- SIROP SPORT CITROR BTL 1L
- BRETS CHIPS POULET BRAISE 6X25
- RANOU ROTI PORC 6TR 240G
- MINI BABYBEL X12 264G
- IDS CREME CASSIS 20D 70CL
- MT BLANC VANILLE MINI 6X125G
- J.ROZE S.HACHE LETENDR X10 1K
- 1ER PRIX BEURRE 1/2S PQ 500G
- ECR/AD COLOSSE CHOC.BLC4X120
- RANOU ROTI DE PORC 4TR 160G
- PASQUIER BISCOTTE MINC.36T 300
- RANOU JBON MON PARIS DD6T270G
- KINDER PINGUI CHOCOLAT 8X30G
- PASQUIER 12 CROISSANTS 480G

Customer from a dataset of 149 942  
customers of a French retailer

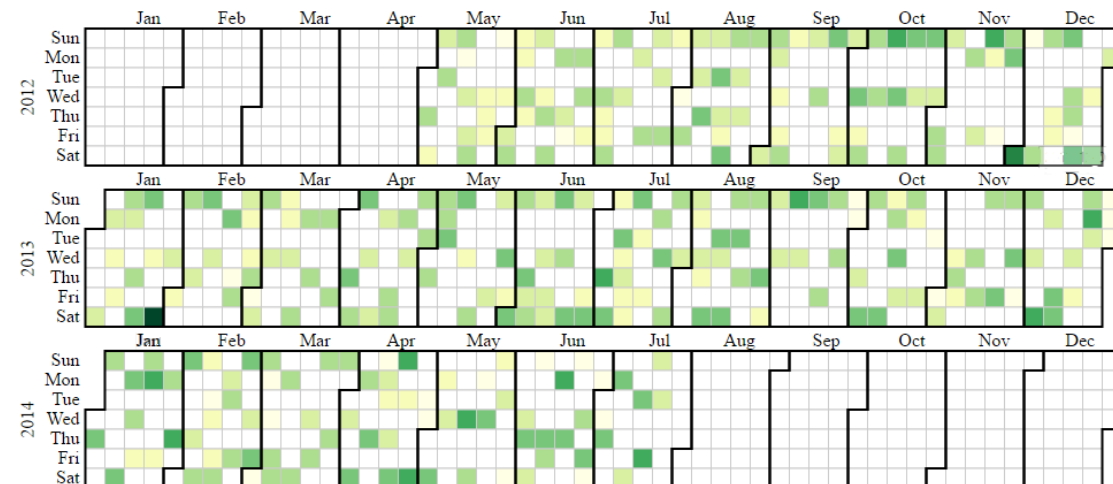


# Signature advantages

- Find regularities in seemingly no regular data
- No window size
- Simple output



Periodic works, signature works



Periodic does not work, signature works



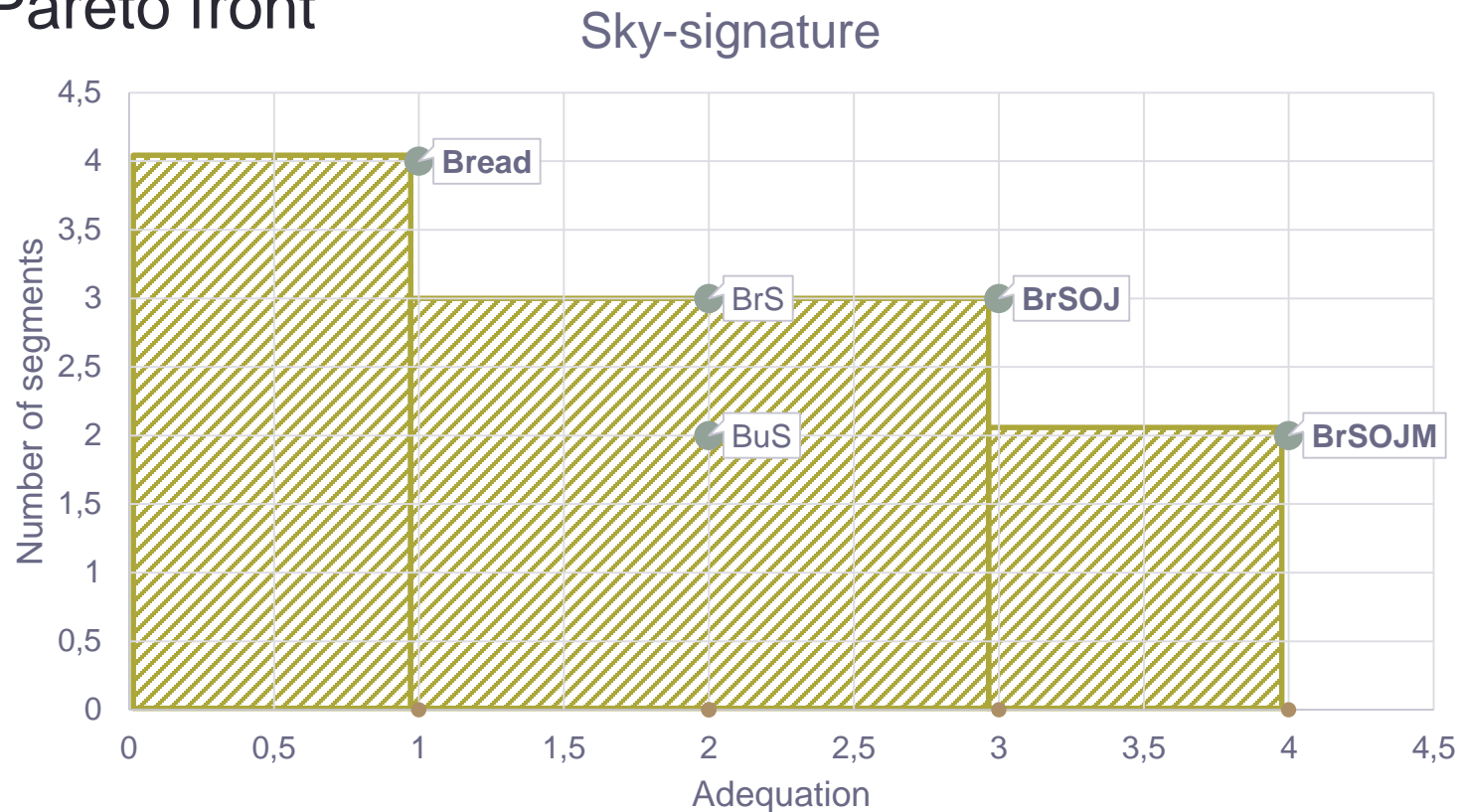
# Sky-signature

- Extension of the signature model
  - How to choose the right number of repetitions?
  - Don't choose, try them all
    - Too many results
    - Pattern selection with a skyline [7]

Timestamp	Receipts
1	Bread, Milk, Orange Juice, Soup
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# Sky-signature

- Sky-signature
  - Compromise between adequation and number of segments
- = Pareto front



# Sky-signature

- Algorithm based on dynamic programming
  - Similar to the sequence segmentation
  - Same complexities as classic signature with  $k = \max\_freq(I)$
- Algorithm based on pattern mining approach
  - Pattern-growth approach  $O(2^{|I|})$

# Sky-signature use case

- Dataset
  - Speeches of D.Trump and H.Clinton in the 2016 presidential campaign
- Objective
  - Find the recurrent topics of each candidate
- Analysis pipeline
  - Apply topic modeling methods on the dataset to get a more abstract overview of each speech main topics
  - Compute the sky-signature on each candidate series of speeches
  - Analyze!

# Sky-signature use case

- Politician signatures

- “Hierarchy” of main topics

Clinton

No	Recurrences ( $k$ )	Signature topics
1	57	Woman as President
2	30	1 + Future challenges for President
3	16	2 + Communities and police
4	12	3 + Childcare and education

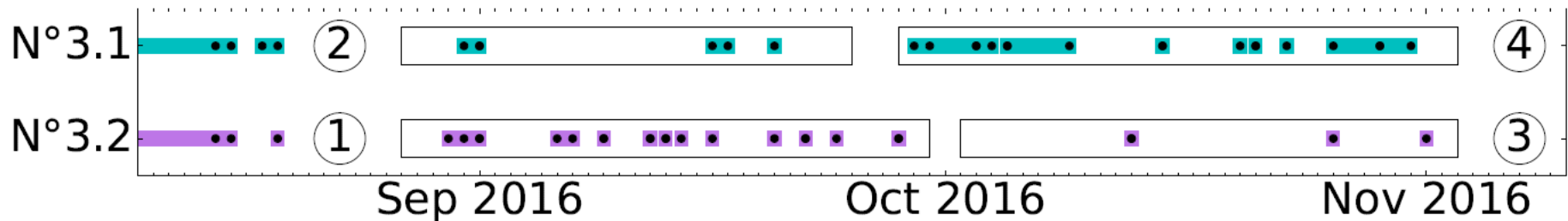
Trump

No	Recurrences ( $k$ )	Signature topics
1	48	Social policy and critics
2	28	1 + New economic policy
3.1	15	2 + Illegal immigration
3.2	15	2 + Education policy
4.1	9	3.2 + Illegal immigration (3.1 + 3.2)
4.2	9	3.2 + Money and wall at border

# Sky-signature use case

- Information from segments

Trump		
No	Recurrences ( $k$ )	Signature topics
1	48	Social policy and critics
2	28	1 + New economic policy
3.1	15	2 + Illegal immigration
3.2	15	2 + Education policy
4.1	9	3.2 + Illegal immigration (3.1 + 3.2)
4.2	9	3.2 + Money and wall at border



- Segment **size** and **frequency** provides information

# Conclusion

- Signatures
  - Find regularities in data, with no constraint on the periodicity
  - No window size
- Sky-signatures
  - Removes the frequency parameter
  - More complex model
- Applied signatures on real use cases
  - Retail use case
  - Natural language processing

# Perspectives

- Add quantities in the model
- Get rid of the number of segments parameter
  - First steps with MDL encoding



Thank you for your attention

Questions?